
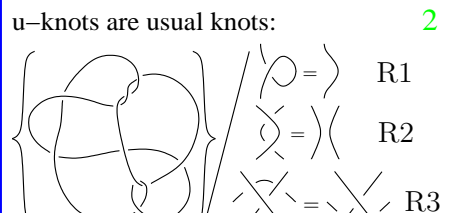

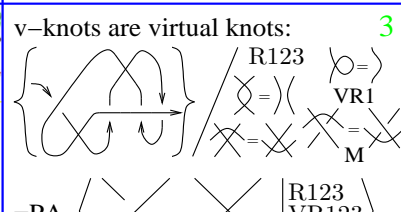

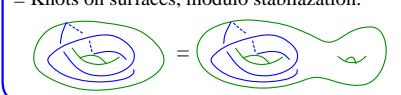
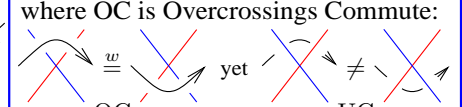
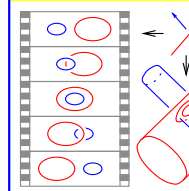
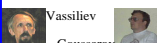
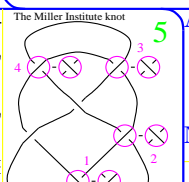
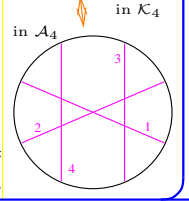
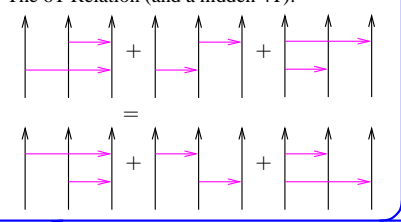



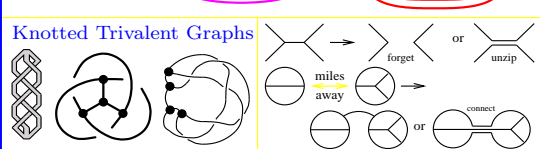


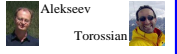


<p style="writing-mode: vertical-rl; transform: rotate(180deg);">topology</p>	<p>1  <b>u-knots</b></p> <p>u-knots are usual knots:</p>  <p>=PA <math>\langle \text{R123} \rangle_0</math> legs </p> <p>"Knots in <math>\mathbb{R}^3</math>"</p>	<p>1+1 <b>v-knots</b></p> <p>v-knots are virtual knots:</p>  <p>=PA <math>\langle \text{R123 VR123} \rangle_0</math></p> <p>=CA <math>\langle \text{R123} \rangle_0</math> </p> <p>= Knots on surfaces, modulo stabilization:</p> 	<p>onto <b>w-knots</b></p> <p>w is for welded, weakly v, and warmup:</p> <p>4 <math>\{\text{w-knots}\} = \{\text{v-knots}\} / (\text{OC})</math></p> <p>where OC is Overcrossings Commute:</p>  <p>Related to "movies of flying rings" to knotted tubes in 4-space, and to "basis conjugating automorphisms of free groups".</p> <p></p> <p>McCool Goldsmith Fenn Rimanyi Rourke Satoh Brendle Hatcher</p>
	<p>combinatorics</p> <p>Extend any <math>V : \{\text{u-knots}\} \rightarrow \mathcal{A}</math> to "singular u-knots" using <math>V(\bowtie) := V(\times) - V(\oslash)</math>, and think "differentiation".</p> <p>Declare "<math>V</math> is of type <math>m</math>" iff <math>V^{(m+1)} \equiv 0</math>, think "polynomial of degree <math>m</math>".</p> <p><math>W = V^{(m)}</math> roughly determines <math>V</math>; <math>W \in \mathcal{A}_m^* = (\mathcal{K}_m / \mathcal{K}_{m+1})^*</math> with</p> <p><math>\mathcal{A}_m := \left\{ \begin{array}{c} \text{m chords} \\ \text{diagram} \end{array} \right\} / \text{4T} = \text{diagram}</math></p> <p>Need an expansion <math>Z : \{\text{u-knots}\} \rightarrow \mathcal{A} = \bigoplus \mathcal{A}_m</math>.</p> <p></p>	<p>5 </p> <p>The Miller Institute knot</p> <p>in <math>\mathcal{A}_4</math> </p>	<p>6 All the same, except</p> <p><math>V(\bowtie) := V(\times) - V(\oslash)</math></p> <p><math>V(\oslash) := V(\times) - V(\bowtie)</math></p> <p><math>\mathcal{A}^v := \{\text{"arrow diagrams"}\} / 6T</math></p> <p>Need a <math>Z : \{\text{v-knots}\} \rightarrow \mathcal{A}^v</math>.</p> <p>The 6T Relation (and a hidden 4T):</p> 
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">low algebra</p>	<p>10 <b>Similar</b></p> <p>with metrized Lie algebras replacing arbitrary Lie algebras</p> <p></p>	<p>9 <b>Similar</b></p> <p>with Lie bi-algebras replacing arbitrary Lie algebras</p> <p></p>	<p>8 <b>Theorem.</b> <math>\mathcal{A}^w \cong \mathcal{A}^{wt} :=</math></p> <p><math>\left\{ \begin{array}{c} \text{only} \\ \text{diagram} \end{array} \right\} / \left( \begin{array}{c} \text{diagram} \\ \text{diagram} \end{array} \right) \text{ \&amp;TC}</math></p> <p>This screams, if you speak the language, <b>LIE ALGEBRAS</b>. And indeed we have</p> <p><b>Theorem.</b> Given a finite dimensional Lie algebra <math>\mathfrak{g}</math>, there is <math>T : \mathcal{A}^w \rightarrow \mathcal{U}(I\mathfrak{g}) := \mathcal{U}(\mathfrak{g} \ltimes \mathfrak{g}_{ab}^*)</math>.</p>
	<p>11 <b>Knots are the wrong objects to study in knot theory!</b> They are not finitely generated and they carry no interesting operations.</p> <p></p> <p><b>Knotted Trivalent Graphs</b></p>  <p><b>Theorem (~).</b> A homomorphic <math>Z</math> is the same as a "Drinfel'd Associator". </p>	<p>13 <b><math>Z</math> is a Quantum Group?</b></p> <p>More precisely, a homomorphic <math>Z</math> ought to be equivalent to the Etingof-Kazhdan theory of deformation quantization of Lie bialgebras.</p> <p></p> <p><b>Dror's Dream: Straighten and fatten this column.</b></p> <p><b>An Idle Question.</b> Is there physics in this column?</p>	<p>12 <b>Switch to w-knotted trivalent tangles,</b></p> <p>wKTT := <math>CA \langle \bowtie, \oslash, Y \rangle</math>.</p> <p><b>Theorem (~).</b> A homomorphic <math>Z</math> is equivalent to proving the Kashiwara-Vergne statement.</p> <p><b>Statement (~, KV, 1978)</b> (proven Alekseev-Meinrenken, 2006). Convolutions of invariant functions on a group match with convolutions of invariant functions on its Lie algebra: for any finite dim. Lie group <math>G</math> with Lie algebra <math>\mathfrak{g}</math>,</p> <p><math>(\text{Fun}(G)^{\text{Ad } G}, \star) \cong (\text{Fun}(\mathfrak{g})^{\text{Ad } G}, \star)</math>.</p> <p>(Closely related to the "orbit method" of representation theory). </p>