(1) Let U be an orthogonal $n \times n$ matrix with $\det(U) = 1$. Prove that there exists a skew-symmetric real matrix A such that $U = e^A$.