

- (1) Solve the following quadratic equation

$$z^2 + (2i - 1)z - 2i = 0.$$

- (2) Let $P(z)$ be a polynomial with real coefficients.

Prove that if z_0 is a root of $P(z)$ then $\bar{z}_0$ is also a root of $P(z)$.

- (3) Express the following number as $a + bi$ for some real a, b :

$$\frac{(3 - \sqrt{3}i)^{71}}{(1 - i)^{53}}$$

- (4) Find all complex solutions of the following equation

$$x^6 + 7x^3 - 8 = 0$$

- (5) Prove that for any complex numbers z_1, z_2, z_3 we have

$$(z_1 z_2) z_3 = z_1 (z_2 z_3)$$

- (6) Let $z = \frac{(1+3i)^{150}}{(2+2i)^{50}(3+4i)^{75}}$

Find $|z|$.