There is only one

A Möbius band for those who want to become one with one.

"One One" was a racehorse,
"One Two" was one too.
"One One" won one race.
12112

1 Motivation

In their 1985 single, "One Vision", the British rock band *Queen* outlined the following research program:

So give me your hands,
Give me your hearts,
I'm ready!
There's only one direction
One world and one nation
Yeah, one vision

– Queen, "One Vision"

Today, **there is only one.**

1 Foundations

Definition 1.1.

For anyone,

$$1+1=1$$
$$1-1=1$$
$$1\div 1=1$$
$$1\times 1=1$$

There is only one function, and it is 1-to-1.

$$f(1)=1$$

and one relation: $1=1$

In particular, $1<1$, and there is only one set:

$$\{1\}$$

Coincidentally, this set is also a field.

1 Calculus

Theorem 1.1. *Every sequence converges.*

Proof. Consider a sequence: $1, 1, \ldots$, and let $\varepsilon = 1$ be arbitrary, we have:

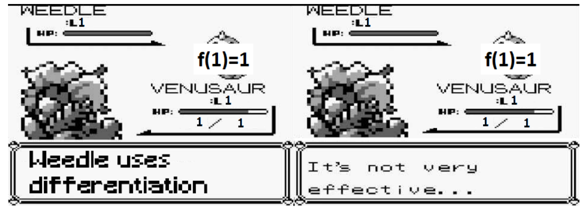
$$|1-1| = |1| = 1 < 1 = \varepsilon$$

Thus, the sequence converges and the limit is 1. □

Corollary 1.1. *Every series converges.*

This is left as an exercise to the reader.

1 Derivatives



$$f'(1) = \lim_{h\to 1} \frac{f(h)-f(1)}{h-1}$$
$$= \lim_{1\to 1} f(1) - f(1) = \lim_{1\to 1} 1 = 1$$

1 Topology and Geometry

Here is a true statement:

There exist manifolds, M^m and N^n with $n>m$, and with $N = M \setminus \{*\}$

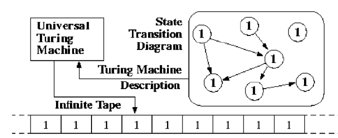
Q: What do you call the empty manifold?
A: Pointless.
Q: How many covers does the empty manifold have with the topology?
A: One.

Theorem 1.1. *Every manifold is algebraic*

Proof. Every manifold can be realized as the solution set to the polynomial equation $1=1$. □

1 Complexity

One makes computers efficient if one removes the useless 0's between the 1's.



Corollary 1.1. *The halting problem is solvable.*

Proof. Halt at 1. □

1 Algebra

There is only one group. Hey look! It's your friend group!

You
•

There is only one ring.

Did you miss it?
Sauron sure did.

1 Yang-Mills Mass Gap

We wish to prove that for any compact simple gauge group G, a non-trivial quantum Yang-Mills theory exists on $\mathbb{R}^1$ and has a mass gap $\Delta > 1$.
Let $G = \{1\}$. It turns out that there is only one quantum Yang-Mills theory on $\mathbb{R}^1$, and it is trivial.
Surprisingly, this trivial Yang-Mills theory has mass gap 1, and $1 > 1$, so the conjecture is almost true.

No further research is required.

1 Poincaré Conjecture

Here is another true statement

There is only one manifold: $\{1\}$

Proof. Every manifold is locally homeomorphic to $\{1\}$, by the (smooth) function $f(1) = 1$. One can extend this homeomorphism to a global homeomorphism by setting $f(1) = 1$. $\square$

Corollary 1.1. *Let M be a simply-connected, closed 1-manifold. Then M is homeomorphic to $\{1\}$.*

There are also other proofs of this fact which use Ricci Flow with surgery.

1 Hodge Conjecture

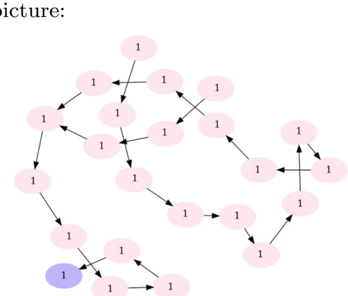
Let M be a complex Kȧhler manifold, with cohomology ring:

$$H^1(M,1) = \bigoplus_{1+1=1}^{1} H^{1,1}(M) = 1$$

Let $N \subseteq M$ be a submanifold representing a class in $H^{1,1}(M)$. We know that $N = \{1\}$, and by Theorem 1.1, N is algebraic.
One concludes that all cohomology classes in $H^{1,1}(M)$ come from subvarieties.

1 Bonus: Collatz Conjecture

Proof by picture:



1 The Riemann Hypothesis

Consider the function:

$$\zeta(s) = \sum \frac{1}{n^s}$$

The above series converges, by Corollary 1.1. We wish to find the roots of ζ. That is, we wish to find places where $\zeta(s) = 1$. Plug in $s = 1$, to and we're done.

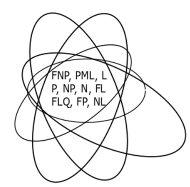
This has many important applications in the distribution of the single prime number, 1.

1 P vs. NP

One gives a solution to the Boolean satisfiability problem:

```
True=1, False=1, Formula=1
```

In fact, every decision problem is in $O(1)$.



1 Navier Stokes

$$\rho\frac{DV}{Dt} = -\nabla p + \nabla \cdot \tau + \rho g$$

Wow, this simplifies greatly[1]

$$1\frac{Df}{D1} = -\nabla 1 + \nabla \cdot 1 + 1$$

In particular, the solution $f(1) = 1$ is smooth, and works in sub- or super-critical spaces.

[1] see Section 1 for more details

1 BSD Conjecture

Dear reader,
I'll be perfectly honest with you and tell you outright that I have no idea what the BSD conjecture even talks about.
I've heard some things about heights of elliptic curves. I've heard of number fields, and ranks of L-functions, but it's all nonsense to me.
All I know that the BSD conjecture holds true over the field with one element, and that's all that's important.
Sincerely,

– Assaf Bar-Natan