### **Administrative Announcements**

- us Class will "meet" at 2:10pm MWF on BB Collaborate
- us Classes will all be recorded
- me My office hour times are now after every class, and will be held on BB Collaborate
- me In-Class TopHat is ungraded, and is replaced by assigned TopHat questions
- you Pre-reading, WeBWork stay the same
- you Watch the videos on the main site!

# S9.2 – Geometric Series

### Assaf Bar-Natan

"If I could only reach you If I could make you smile, If I could only reach you, That would really be a breakthrough."

- "Breakthru", Queen

March 16, 2020

March 16, 2020 - S9.2 - Geometric Series

Assaf Bar-Natan 2/13

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We've seen sequences:

 $a_1, a_2, a_3, \ldots$ 

Now, we're going to add them up:

 $a_1$   $a_1 + a_2$  $a_1 + a_2 + \dots + a_n + \dots$ 

Such a sum is called a series.

## Takeaway

Q: What is the difference between a sum and a series?

**Q**: What is the difference between a **sum** and a **series**? A sum only adds up finitely many elements, but a series adds up ininitely many elements. **Q:** What is the difference between a **sum** and a **series**? A sum only adds up finitely many elements, but a series adds up ininitely many elements.

 $\sum_{i=0}^n f(x_i) \Delta x$ 

is a sum.

$$\sum_{n=0}^{\infty} \frac{1}{2^n}$$

is a series (see Zeno's Paradox video)

A geometric series is characterized by...





## Takeaway

A geometric series is a special kind of series, where the ratio between subsequent terms is constant.

Marzipan is modeling the mouse population in the barn. She finds three mice in the barn, and measures that the number of mice is multiplied by a factor of 1.3 every week. She writes:

"I want to know how many mice will be in the barn by summertime. If summer many many weeks away, I'll approximate using the formula for the inifinite geometric series to get:

number of mice = 
$$3 + 3(1.3) + 3(1.3)^2 + \dots = \frac{3}{1 - 1.3} = -10$$

So there will be -10 mice over the summer."

Can you help Marzipan interpret her answer?



# Plans for the Future

For next time: Do WeBWork 9.3 and actively read section 9.3



#### What is the area of the shaded region?



✓ 55% Answered Correctly



### $\text{Write the limit of the sequence } \{1, 1.1, 1.11, 1.111, 1.1111, 1.11111, 1.11111, \dots\} \text{ as a series}.$

✓ 60% Answered Correctly



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#### Write the limit of the sequence $\{0.9, 0.99, 0.999, 0.9999, 0.99999, \ldots\}$ as a series.

