## Welcome to MAT136 LEC0501 (Assaf)

## Administrative Announcements

us Class will "meet" at $2: 10 \mathrm{pm}$ MWF on BB Collaborate
us Classes will all be recorded
me My office hour times are now after every class, and will be held on BB Collaborate
me In-Class TopHat is ungraded, and is replaced by assigned TopHat questions
you Pre-reading, WeBWork stay the same
you Watch the videos on the main site!

# S9.2 - Geometric Series 

## Assaf Bar-Natan

"If I could only reach you
If I could make you smile,
If I could only reach you,
That would really be a breakthrough."
-"Breakthru", Queen
March 16, 2020

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## Series

We've seen sequences:

$$
a_{1}, a_{2}, a_{3}, \ldots
$$

Now, we're going to add them up:

$$
\begin{aligned}
& a_{1} \\
& a_{1}+a_{2} \\
& a_{1}+a_{2}+\cdots+a_{n}+\cdots
\end{aligned}
$$

Such a sum is called a series.

## Takeaway

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$$
\sum_{i=0}^{n} f\left(x_{i}\right) \Delta x
$$

is a sum.

$$
\sum_{n=0}^{\infty} \frac{1}{2^{n}}
$$

is a series (see Zeno's Paradox video)

A geometric series is characterized by...
A The terms in the sum are constant ..... 6
B The ratios of subsequent terms in the sum is a fixed number ..... 75
C The differences between subsequent terms in the sum is a fixed number ..... 11
D Every term in the sum is a constant multiple of all the previous terms ..... 26
E The terms in the sum are increasing ..... 0

| March 15 at 10:34 PM results |  |  | Segment Results |  |  | Compare with session |  |  |  | Show percentages | Hide Graph | Condense Text |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 118/120 answered |  |  |  |  |  |  |  |  |  |  |  | CAsk Again |  |
| $\wedge$ | $<$ | > |  | Open | $\theta$ |  | 三 Responses | $\checkmark$ Correct | > |  |  | Q 88\% | 」 7 |

## Takeaway

A geometric series is a special kind of series, where the ratio between subsequent terms is constant.

## Marzipan's Problem

Marzipan is modeling the mouse population in the barn. She finds three mice in the barn, and measures that the number of mice is multiplied by a factor of 1.3 every week. She writes:
"I want to know how many mice will be in the barn by summertime. If summer many many weeks away, I'll approximate using the formula for the inifinite geometric series to get:
number of mice $=3+3(1.3)+3(1.3)^{2}+\cdots=\frac{3}{1-1.3}=-10$
So there will be -10 mice over the summer."
Can you help Marzipan interpret her answer?

## 7 <br> Submissions Closed

Which of the following add up to 10 ?

| A $\sum_{n=0}^{\infty} \frac{9}{10^{n}}$ |  | ${ }^{68}$ |
| :---: | :---: | :---: |
| $\mathrm{B}_{\mathrm{B}} \sum_{\mathrm{n}=0}^{\infty} \frac{\mathrm{m}^{10}}{}$ | $\square$ | 15 |
| c $\sum_{n=0}^{\infty} \frac{9^{n}}{10^{n}}$ | - | 28 |
| - $\sum_{n=0}^{\infty} \frac{9}{10}$ | I | 3 |



## Plans for the Future

For next time:
Do WeBWork 9.3 and actively read section 9.3

What is the area of the shaded region?


A $\pi$


15
B $\frac{2 \pi}{3}$
75
C $\frac{4 \pi}{3}$
24

D $\infty$
23

| Invalid da | , |  | Results | Compare with session |  |  |  |  |  | Show percentages | Hide Graph | Conden | Text |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 137/137 answered $\square_{\text {Ask Again }}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\wedge$ | $<$ | > | - |  | $\theta$ closed | 三 Responses |  | Correct | > |  |  | Q 88\% | 7 |

## " Submissions Closed

Write the limit of the sequence $\{1,1.1,1.11,1.111,1.1111,1.11111,1.111111, \ldots\}$ as a series.


Write the limit of the sequence $\{0.9,0.99,0.999,0.9999,0.99999, \ldots\}$ as a series．

|  |  |  |  |  |  |  | $\checkmark$ 45\％Answered Correctly |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | $\sum_{n=0}^{\infty}$ | $(0.9)^{\mathrm{n}}$ |  |  |  |  |  |  | 7 |  |
| B | $\sum_{n=0}^{\infty}$ | $9(0.1)^{n}$ |  |  |  |  |  |  | 45 |  |
| C | $\sum_{n=0}^{\infty}$ | $0.9(1)^{r}$ |  |  |  |  |  |  | 23 |  |
| D | $\sum_{n=0}^{\infty}$ | $0.9(0.1$ |  |  |  |  |  |  | 61 |  |
| Invalid date | －Se | Segment Results co | mpare with sessio |  |  |  | Show percentages | Hide Graph | h Condens | e Text |
| 136／136 an | nswered |  |  |  |  |  |  |  | $\mathrm{Cl}^{\text {ask }}$ | Again |
| $\wedge$ | ＜＞ | －Open | $\theta$ Closed | 三 Responses | $\checkmark$ Correct | 》 |  |  | Q $88 \%$ | $\xrightarrow{\text { 」 }}$ |

