Kasra Rafi

Curriculum Vitae

Academic Positions

- 2018–present **Professor**, University of Toronto
- 2012-present Member of School of Graduate Studies, University of Toronto
 - 2019–2021 Associate Chair (Graduate), University of Toronto
 - 2015–2018 Associate Professor, University of Toronto
 - 2012–2015 Assistant Professor, University of Toronto
 - 2008–2012 Assistant Professor, University of Oklahoma
 - 2007–2008 L.E. Dickson Instructor, University of Chicago
 - 2004–2007 Postdoctoral Fellow, University of Connecticut
 - 2001–2004 Ky Fan Visiting Assistant Professor, University of California Santa Barbara

Visiting Positions

Fall 2022	Visiting Professor, University of Chicago
Fall 2016	Simons Visiting Professor, Mathematical Sciences Research Institute
May–Aug 2010	Hausdorff Research Institute for Mathematics
Jan–Jul 2009	Clay Research Scholar, University of Chicago
Fall 2007	Mathematical Sciences Research Institute
Jul–Aug 2003	Isaac Newton Institute for Mathematical Sciences, University of Cambridge, UK

Education

2001 Ph.D., Mathematics, Stony Brook University, Stony Brook, NY
1995 B.Sc., Mathematics, Sharif Institute of Technology, Tehran, Iran

Fields of Interest

Geometry and dynamical properties of Teichmüller space Geometric group theory, in particular, mapping class group and $Out(\mathbb{F}_n)$ Low dimensional Geometry and Topology

Grants and Recognitions

- 2024 Fellow of American Mathematical Society
- 2021–2022 Simons Fellow in Mathematics
 - 2020 Fields Institute Fellow
- 2018–2024 NSERC Discovery grant, RGPIN 06486
- Fall 2016 Simons Visiting Professor at MSRI
- 2013–2018 NSERC Discovery grant, RGPIN 435885
- 2010–2013 NSF Research Grant PI, DMS-1007811
- Jan-Aug 2009 Clay Research Scholar, University of Chicago
 - 2001 James Simons Prize for Excellence in Research, Stony Brook University
 - 1992 Silver Medal, International Mathematics Olympiad, Moscow

Research papers

Preprints

- 2023 Random walks on groups and superlinear divergent geodesics, Kunal Chawla, Inhyeok Choi and Vivian He
- 2022 **Fibered 3-manifolds and Veech groups**, with Christopher J. Leininger, Nicholas Rouse, Emily Shinkle and Yvon Verberne
- 2022 Genericity of sublinearly Morse directions in CAT(0) spaces and the Teichmüller space, with Ilya Gekhtman and Yulan Qing
- 2021 Asymptotic Dimension of Big Mapping Class Groups, with Curtis Grant and Yvon Verberne

To Appear

- 2022 **Two results on end spaces of infinite type surfaces**, with Kathryn Mann, Kasra Rafi, to appear in Michigan Mathematical Journal
- 2020 **Sub-linearly Morse Boundary II: Proper Geodesic Spaces**, *with Yulan Qing and Giulio Tiozzo*, to appear in Geometry & Topology

Published

- 2023 Large Scale Geometry of Big Mapping Class Groups, with Kathryn Mann, Geometry & Topology 27 (2023), 2237–2296
- 2022 **Big mapping class groups with hyperbolic actions: classification and applications**, *with Camille Horbez and Yulan Qing*, Journal of the Institute of Mathematics of Jussieu **21** (2022), no. 6, 2173–2204
- 2022 **Benjamini-Schramm convergence of periodic orbits**, *with Amir Mohammadi*, Geometriae Dedicata **216** (2022), no. 5, Paper No. 57
- 2022 **Sub-linearly Morse Boundary I: CAT(0) Spaces**, with Yulan Qing and Giulio Tiozzo, Advances in Mathematics **404** (2022), part B, Paper No. 108442
- 2022 Expected covering radius of a translation surface, with Howard Masur and Anja Randecker, International Mathematics Research Notices 2022, no. 10, 7967–8002
- 2022 Local maxima of the systole function, with Maxime Fortier Bourque, Journal of the European Mathematical Society (JEMS) 24 (2022), no. 2, 623–668
- 2021 Geodesics in the Mapping Class Group, with Yvon Verberne, Algebraic & Geometric Topology **21** (2021), no. 6, 2995–3017
- 2021 **Convexity of balls in the outer space**, *with Yulan Qing*, Groups, Geometry, and Dynamics **15** (2021), no. 3, 893–934
- 2021 Quasi-geodesics in $Out(\mathbb{F}_n)$ and their shadows in sub-factors, with Yulan Qing, Journal of the London Mathematical Society (2) **104** (2021), no. 1, 147–168

- 2020 Centralizers in Mapping Class Group and decidability of Thurston Equivalence, with Nikita Selinger and Michael Yampolsky, Arnold Mathematical Journal 6 (2020), no. 2, 271–290
- 2020 Renormalizing an infinite rational IET, with W. Patrick Hooper and Anja Randecker, Discrete and Continuous Dynamical Systems - Series A (2020), 40, no. 9, 5105–5116
- 2020 Coarse and fine geometry of the Thurston metric, with David Dumas and Anna Lenzhen and Jing Tao, Forum of Mathematics, Sigma 8 (2020), paper no. e28, 58 pages
- 2020 Isomorphisms between big mapping class groups, with Juliette Bavard and Spencer Dowdall, International Mathematics Research Notices (2020), no. 10, 3084–3099
- 2020 Limit sets of Weil-Petersson geodesics with non-minimal ending laminations, with Jeffrey Brock, Chris Leininger and Babak Modami, Journal of Topology and Analysis 12 (2020), no. 1, 1–28
- 2020 Limit sets of Teichmüller geodesics with minimal non-uniquely ergodic vertical foliation
 II, with Jeffrey Brock, Chris Leininger and Babak Modami, Journal für reine und angewandte Mathematik, **758** (2020), 1–66
- 2019 Limit sets of Weil-Petersson geodesics, with Jeffrey Brock, Chris Leininger and Babak Modami, International Mathematics Research Notices (2019), no. 24, 7604–7658
- 2019 Geodesic Currents and Counting Problems, with Juan Souto, Geometric and Functional Analysis 29 (2019), no. 3, 871–889
- 2019 **Counting closed geodesics in strata**, *with Alex Eskin and Maryam Mirzakhani*, Inventiones Mathematicae **215** (2019), no. 2, 535–607
- 2018 **Teichmüller geodesics with** *d***-dimensional limit sets**, *with Anna Lenzhen and Babak Modami*, Journal of Modern Dynamics **12** (2018), 261–283
- 2018 **Rigidity of Teichmüller space**, with Alex Eskin and Howard Masur, Geometry & Topology **22** (2018), no. 7, 4259–4306
- 2018 Non-convex balls in the Teichmüller metric, with Maxime Fortier Bourque, Journal of Differential Geometry **110** (2018), no. 3, 379–412
- 2018 Algebraic ending laminations and quasi-convexity, with Mahan Mj, Algebraic & Geometric Topology **18** (2018), no. 4, 1883–1916
- 2018 Limit sets of Teichmüller geodesics with minimal non-uniquely ergodic vertical foliation, with Chris Leininger and Anna Lenzhen, Journal für die reine und angewandte Mathematik 737 (2018), 1–32
- 2017 Uniform fellow traveling between surgery paths in the sphere graph, with Matt Clay and Yulan Qing, Algebraic & Geometric Topology 17, (2017), no. 6, 3751–3778
- 2017 Large scale rank of Teichmülcer space, with Alex Eskin and Howard Masur, Duke Mathematical Journal **166** (2017), no. 8, 1517–1572

2016	Uniform growth rate , <i>with Jing Tao</i> , Proceedings of the American Mathematical Society 144 (2016), no. 4, 1415–1427
2015	The shadow of a Thurston geodesic to the curve graph , with Anna Lenzhen and Jing Tao, Journal of Topology 8 (2015), no. 4, 1085–1118
2015	Digraphs and cycle polynomials for free-by-cyclic groups , with Yael Algom-Kfir and Eriko Hironaka, Geometry & Topology 19 (2015), no 2, 1111–1154
2015	Mapping tori of small dilatation expanding train-track maps, with Yael Algom Kfir, Topology and its Applications 180 (2015), 44–63
2014	Uniform hyperbolicity of the curve graph via surgery sequences , with Matt Clay and Saul Schleimer, Algebraic & Geometric Topology 14 (2014), no. 6, 3325–3344
2014	Hyperbolicity in Teichmüller space, Geometry & Topology 18 (2014), no 5, 3025–3053
2014	On hyperbolicity of free splitting and free factor complexes , with Ilya Kapovich,
	Groups, Geometry, and Dynamics 8 (2014), no. 2, 391–414
2013	Diameter of the thick part of moduli space, with Jing Tao, Duke Mathematical Journal 162 (2013), no. 10, 1833–1876
2012	Bounded combinatorics and the Lipschitz metric on Teichmüller space, with Anna Lenzhen and Jing Tao, Geometriae Dedicata 159 (2012), 353–371
2012	Grafting rays fellow travel Teichmüller geodesics , with Young-Eun Choi and David Dumas, International Mathematics Research Notices (2012), no. 11, 2445–2492
2011	Length of a curve is quasi-convex along a Teichmüller geodesic, with Anna Lenzhen, Journal of Differential Geometry 88 (2011), no. 2, 267–295
2011	Curve complexes are rigid , with Saul Schleimer, Duke Mathematical Journal Volume 158 (2011), no 2, 225–246
2010	Length spectra and degeneration of flat metrics, with Moon Duchin and Christopher Leininger, Inventiones Mathematicae, 182 , (2010) no. 2, 231–277
2009	Divergence rate of geodesics in Teichmüller space and mapping class groups , <i>with Moon Duchin</i> , Geometric and Functional Analysis 19 (2009), no. 3, 722–742
2009	Covers and the curve complex, with Saul Schleimer, Geometry & Topology 13 (2009), no. 4, 2141–2162
2008	Lines of minima and Teichmüller geodesics, with Young-Eun Choi and Caroline Series, Geometric and Functional Analysis 18 (2008), no. 3, 698–754
2008	Lines of minima are uniformly quasigeodesic, with Young-Eun Choi and Caroline Series, Pacific Journal of Mathematics 237 (2008), no. 1, 21–44

- 2007 Comparison between Teichmüller and Lipschitz metrics, with Young-Eun Choi, Journal of the London Mathematical Society (2) 76 (2007), no. 3, 739–756
- 2007 **A combinatorial model for the Teichmüller metric**, Geometric and Functional Analysis **17** (2007), no. 3, 936–959
- 2007 Thick-thin decomposition for quadratic differentials, Mathematical Research Letters **14** (2007), no. 2, 333–341
- 2005 **A** characterization of short curves of a Teichmüller geodesic, Geometry & Topology **9** (2005), 179–202

Invited Talks

Lecture Series

- June 2023 Mirzakhani's integration formula for the volume of moduli space, Geometry and spectra of random hyperbolic surfaces, Université de Montréal
- May 2023 Combinatorial Teichmüller Theory, Beijing International Center for Mathematicial Reasearch
- March 2022 Course Geometry of Big Mapping Class Groups, Shanghai Center for Mathematical Sciences
- March 2022 Sublinearly Morse Boundary, A Week at Infinity, Online workshop

Recent Conferences

- July 2023 Erwin Schrödinger International Institute for Mathematics, Vienna, Austria, Geometric and Asymptotic Group Theory with Applications 2023 - Groups and Dynamics
- January 2023 University of Utah, Slat Lake City, Salt Flat: A research community in Teichmüller dynamics
- December 2022 PIMS, Vancouver, The 2022 Pacific Rim Mathematical Association Congress
 - Sept. 2022 CIRM, Marseille Luminy, France, Dynamics and Geometry on Moduli Spaces conference
 - August 2022 Park City, Utah, Wasatch Topology Conference
 - April 2022 AIM, San Jose, Random walks beyond hyperbolic groups
 - January 2020 Tsinghua Sanya International Mathematics Forum, Sanya, China, Frontier of Analysis and Geometry of Teichmüller Spaces
 - June 2019 Bowdoin College, Brunswick, Boundaries of Random Walks and Applications
 - August 2018 Fields Institute, Toronto, Workshop on Geometry of Teichmüller Space
 - July 2018 Peking University, Beijing, A conference on Geometric Group Theory
 - June 2018 Fields Institute, Toronto, 2018 Fields Institute Annual General Meeting
 - May 2018 Stanford University, Palo Alto, The Mathematical Legacy of Maryam Mirzakhani
 - April 2018 University of Warwick, Coventry, Geometry of Teichmüller space and mapping class groups
 - Nov. 2017 ICTS, Bangalore, Surface group representation and geometric structures
 - Sept. 2017 Ventotene, Italy, Moduli Space
 - August 2017 Trinity College, Dublin, Geometry and Dynamics of Moduli Spaces
 - June 2017 Newton Institute, Cambridge, Group actions and cohomology in non-positive curvature
 - May 2017 Vanderbilt University, Vanderbilt, Shank Conference
 - April 2017 University of Arkansas, Fayetteville, Redbud Topology Conference
 - Feb. 2017 CIRM, Marseille, Dynamics and Geometry in the Teichmüller Space
 - October 2016 **MSRI**, *Berkeley*, Geometry of mapping class groups and $Out(\mathbb{F}_n)$
 - July 2016 KAIST, Daejeon, Korea, Geometric Topology Fair
 - May 2016 **ICERM**, *Providence*, Effective and Algorithmic Methods in Hyperbolic Geometry and Free Groups
 - May 2016 Casa Matemática Oaxaca, Oaxaca, Mexico, Flat Surfaces and Dynamics of Moduli Space

- Jan. 2016 African Institute for Mathematical Sciences, Cape Town, Quadratic Differentials
- Sept. 2015 Mathematical Institute, Oxford, UK, Geometry and Dynamics on Moduli Spaces
- June 2015 Inter-University Centre Dubrovnik, Dubrovnik, Croatia, Dubrovnik VIII Geometric Topology, Geometric Group Theory & Dynamical Systems
- May 2015 University of Texas at Austin, Austin, Workshop on Mapping Class Groups and $Out(\mathbb{F}_n)$ Online Seminars
- April 2021 Frontiers in Mathematical Sciences, IPM, Iran
- Sept. 2020 Big Surfaces Seminar
- July 2020 Australian Geometric Topology Webinar
- April 2020 Billiards and Surfaces á la Teichmüller and Riemann

Colloquia (Excluding job talks)

- 2023 **Tel Aviv University**, (upcoming)
- 2020 Rice University
- 2019 University of Toronto
- 2017 Pittsburgh University
- 2017 University of Michigan
- 2014 University of Oklahoma
- 2014 University of Indiana
- 2011 University of Arkansas
- 2011 Rice University

Seminars

Brown University, California Institute of Technology, Cornell University, CUNY Graduate Center, Columbia University, Harvard University, Institut des Hautes Études Scientifiques, Joint USC-UCLA-Caltech, Kyoto University, McGill University, Osaka University, Oklahoma State University, Princeton University, Rutgers University, South China University of Technology, Stanford University, Sun Yat-Sen University, SUNY at Stony Brook, Tufts University, Université de Rennes, Université Paris-Sud, University of Connecticut, University of Maryland, University of California at Davis, University of California at Santa Barbara, University of Chicago, University of Illinois at Chicago, University of Illinois at Urbana-Champaign, University of Michigan, University of Southern California, University of Seoul, University of Texas Austin, University of Toronto, University of Utah, University of Warwick, University of Wisconsin, Yale University.

Supervision

Graduate students

- Current Vivian He
- Current Ali Pirhosseinloo
- Current Mohammad Honari
- Current Pooya Honaryar
 - 2022 Assaf Bar-Natan, University of Toronto
 - 2021 Ivan Telpukhovskiy, University of Toronto
 - 2020 Yvon Verberne, University of Toronto
 - 2013 Funda Gültepe, University of Oklahoma
 - 2013 Yoe Alexander Herrera Jaramillo, University of Oklahoma

Undergraduate Research

- 2022 Asha McMullin, (Independent Research)
- 2022 Kunal Chawla, (Supported by NSERC)
- 2021 Vivian He, (Supported by NSERC)
- 2019 Curtis Grant, (Supported by NSERC)
- 2018 Ci Zhang, (Supported by UT Work Study Program)
- 2018 Jordan Hofmann, (Supported by NSERC)
- 2017 Adriano Pacifico, (Supported by NSERC)

Highschool Mentorship

- 2019 Anna Krokhine
- 2018 Clare Radnoff
- 2016 Gemma Zhang
- 2015 Abtin Ameri
- 2015 Andrey Khesin
- 2014 Coco Zhang

Teaching Experience

Undergraduate courses

Pre-calculus, Single and Multivariable Calculus at all levels, Honors Calculus, Ordinary and Partial Differential Equations, Physical Mathematics, Discrete Mathematics, Logic and Proofs, Linear Algebra, Abstract Algebra, Probability, Graph theory, Complex Analysis, General Topology, Knot Theory, Geometric Group theory, Problem Solving Seminar, and Seminar in Mathematics.

Graduate courses

Algebra for Teachers, Geometry for Teachers, Introduction to Hyperbolic Geometry, Algebraic Topology, Differential Topology, Combinatorial Methods and Geometric Literacy.

Topics courses

Kleinian groups, Introduction to Teichmüller Space, Currents and Counting problems, Geometry and Dynamics in Teichmüller Space Equipped with the Thurston Metric.

Recent Professional Activities

May 2023 Co-organizer for the conference: 1,2,3: Curves, Surfaces, and 3-Manifolds, CMS, Haifa, Israel.

- January 2023 Co-organizer for the conference: Salt Flat: A research community in Teichmüller dynamics, University of Utah, Slat Lake City.
 - April 2022 Co-organizer for the conference *Mapping class groups and* $Out(F_n)$, Institut Henri Poincaré, Paris.
 - May 2019 Co-organizer of the workshop Flat Surfaces and Dynamics of Moduli Space, II, Oaxaca.
 - Fall 2018 Co-organizer of the Thematic Program on *Teichmüller Theory and its Connections to Geometry, Topology and Dynamics* Fields Institute, Toronto.
- Nov 2018 Co-organizer for the Fields Symposium in honor of Maryam Mirzakhani, Fields Institute, Toronto.

2018-present Associate Editor for The Journal of Iranian Mathematical Society

- 2016-2019 Associate Editor for The Journal of the Ramanujan Mathematical Society
- 2008-2018 Mentor for Association for Women in Mathematics (AWM) Mentor Network

Collaborators

- Yael Algom-Kfir (University of Haifa)
- Mladen Bestvina (University of Utah)
- Mathew Clay (University of Arkansas)
- Young-Eun Choi
- Moon Duchin (Tufts University)
- Alex Eskin (University of Chicago)
- W Patrick Hooper (CUNY City College)
- Eriko Hironaka (Florida State University)
- Fanny Kassel (IHES)
- Misha Kapovich (Univ. of California Davis)
- Anna Lenzhen (Rennes)
- Howard Masur (University of Chicago)
- Maryam Mirzakhani (Stanford University)
- Amir Mohammadi (UCSD)
- Yulan Qing (University of Tennessee, Anja Randecker (Heidelberg University) Knoxville)
- Nicholas Rouse (Rice University)
- Saul Schleimer (University of Warwick)
- Caroline Series (University of Warwick)
- Jing Tao (University of Oklahoma)
- Yvon Verberne (Western University)

- Juliette Bavard (Rennes)
- Jeffery Brock (Yale University)
- Spencer Dowdall (Vanderbilt University)
- David Dumas (Univ. of Illinois at Chicago)
- O Maxime Fortier Bourque (Université de Montréal)
- Ilya Gekhtman (Technion)
- o Camille Horbez (CNRS, Laboratoire de Mathématiques d'Orsay)
- Ilya Kapovich (CUNY Hunter College)
- Christopher J. Leininger (Rice University)
- Kathryn Mann (Cornell University)
- Babak Modami (Tata Institute)
- Mahan Mj (Tata Institute)
- - Nikita Selinger (University of Alabama)
 - Emily Shinkle (UIUC)
 - Juan Souto (Rennes)
 - Giulio Tiozzo (University of Toronto)
 - Michael Yampolsky (University of Toronto)