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O-Level Paper

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- 1 [4] 2003 dollars are placed into N purses, and the purses are placed into M pockets. It is known that N is greater than the number of dollars in any pocket. Is it true that there is a purse with less than M dollars in it?
- **2** [4] Two players in turns colour the sides of an n-gon. The first player colours any side that has 0 or 2 common vertices with already coloured sides. The second player colours any side that has exactly 1 common vertex with already coloured sides. The player who cannot move, loses. For which n the second player has a winning strategy?
- **3** [5] Points K and L are chosen on the sides AB and BC of the isosceles $\triangle ABC$ (AB = BC) so that AK + LC = KL. A line parallel to BC is drawn through midpoint M of the segment KL, intersecting side AC at point N. Find the value of $\angle KNL$.
- 4 [5] Each term of a sequence of natural numbers is obtained from the previous term by adding to it its largest digit. What is the maximal number of successive odd terms in such a sequence?
- **5** [5] Is it possible to tile 2003×2003 board by 1×2 dominoes placed horizontally and 1×3 rectangles placed vertically?