SOAR into Mathematics—Number Theory
July 24–August 11, 2000
List of Topics (Tentative)

1. *Foundations of Number Theory*
   properties of the integers; divisibility; the Division Algorithm
2. *Greatest Common Divisors*
   greatest common divisors; coprimality; the Diophantine equation $ax + by = 1$; the Euclidean Algorithm; irrationality of $\sqrt{2}$; a geometric detour
3. *Prime Numbers*
   primes; the Fundamental Theorem of Arithmetic; Euclid and the infinitude of primes
4. *Modular Arithmetic*
   congruences; modular arithmetic; congruences and division; solving linear congruences
5. *The Multiplicative Group*
   special properties of arithmetic modulo primes; the Chinese remainder theorem
6. *The Multiplicative Group Modulo n*
   the Euler ϕ-function; Fermat's Little Theorem; multiplicative order; primitive roots; solving radical congruences
7. *Factoring Integers*
   trial division; shortcuts for small primes; Fermat's differences-of-squares method; primality tests; advanced algorithms
8. *Egyptian Fractions*
   the Rhind papyrus; algorithms for Egyptian fraction expansion; the splitting formula; largest and second-largest denominators; contemporary research
9. *Cryptography*
   Diffie–Hellman public key exchange; public-key cryptography; the RSA cryptosystem
10. *Survey of Additive Number Theory*
    sums of two squares; Lagrange's four-squares theorem; representation by three squares; Waring's problem; Twin Primes and Goldbach conjectures

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