

- Today: Integral and comparison tests.
- Homework before Wednesday's class: watch videos 13.13, as well as 13.14.

Rapid questions: For which values of $p \in \mathbb{R}$ are these series convergent?

1.
$$\sum_{n=0}^{\infty} \frac{1}{p^n}$$

2.
$$\sum_{n=0}^{\infty} \frac{1}{n^p}$$

3.
$$\sum_{n=0}^{\infty} p^n$$

4.
$$\sum_{n=0}^{\infty} n^p$$

More rapid questions: Convergent or divergent?

1.
$$\sum_n \frac{n^{10} + 17n^7 + 3}{n^{11}}$$

2.
$$\sum_n \frac{\sqrt[3]{n^2 + 1} + 1}{\sqrt{n^4 + n} + n + 1}$$

Slower questions: convergent or divergent?

$$1. \sum_n \frac{2^n - 40}{3^n - 20}$$

$$2. \sum_n \frac{(\ln n)^{20}}{n^2}$$

$$3. \sum_n \sin^2 \frac{1}{n}$$

$$4. \sum_n \frac{1}{n(\ln n)^3}$$

$$5. \sum_n \frac{1}{n \ln n}$$

$$6. \sum_n e^{-n^2}$$

We know

- $\forall n \in \mathbb{N}, 0 < a_n < 1.$
- the series $\sum_n^{\infty} a_n$ is convergent

Determine whether the following series are convergent, divergent, or we do not have enough information to decide:

1. $\sum_n^{\infty} \sin a_n$

2. $\sum_n^{\infty} \cos a_n$

3. $\sum_n^{\infty} \sqrt{a_n}$