

**Problem 1.** What does the Leibnitz Alternating Series Test state?

**Problem 2** (Spivak 23-1). Determine whether the following converge:

1. 
$$\sum_{n=1}^{\infty} \frac{\sin n\theta}{n^2}$$

5. 
$$\sum_{n=1}^{\infty} \frac{1}{n^2 \log n}$$

2. 
$$\sum_{n=1}^{\infty} (-1)^n \frac{\log n}{n}$$

6. 
$$\sum_{n=2}^{\infty} \frac{1}{(\log n)^k}$$

3. 
$$\frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{5^2} + \frac{1}{7^2} + \frac{1}{11^2} + \frac{1}{13^2} + \dots$$

7. 
$$\sum_{n=2}^{\infty} \frac{1}{(\log n)^n}$$

4. 
$$\sum_{n=1}^{\infty} \frac{2^n n!}{n^n}$$

8. 
$$\sum_{n=1}^{\infty} \frac{n^2}{n^3 + 1}$$

**Problem 3** (Spivak 23-15).

1. Prove if  $\sum a_n$  converges absolutely, then for any subsequence  $a_{n_k}$ ,  $\sum a_{n_k}$  also converges absolutely.
2. Prove if  $\sum a_n$  converges absolutely, then

$$\sum_{n \in \mathbb{N}} a_n = (a_0 + a_2 + a_4 + \dots) + (a_1 + a_3 + a_5 + \dots) \quad (1)$$

**Problem 4** (Spivak 23-16). Prove if  $\sum a_k$  is absolutely convergent, then  $|\sum a_k| \leq \sum |a_k|$ .