

# Euler's Formula for Polyhedra

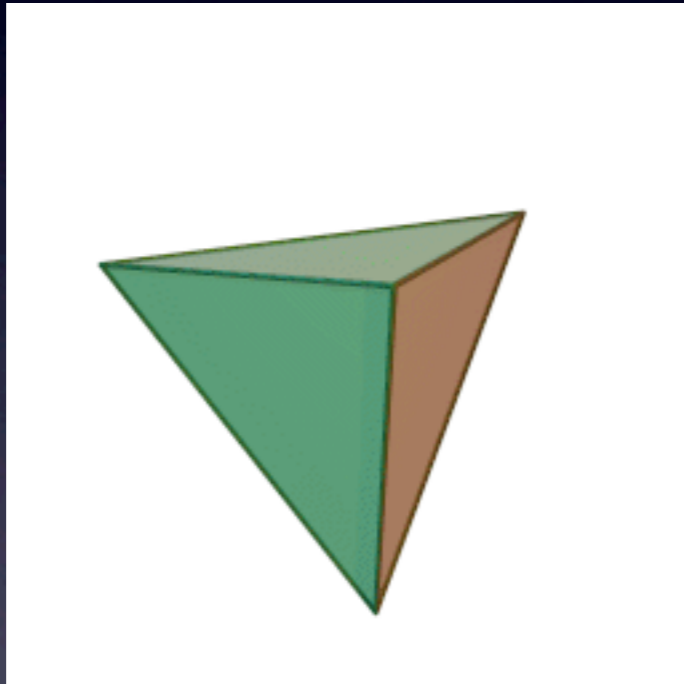


J. Colliander  
U. Toronto

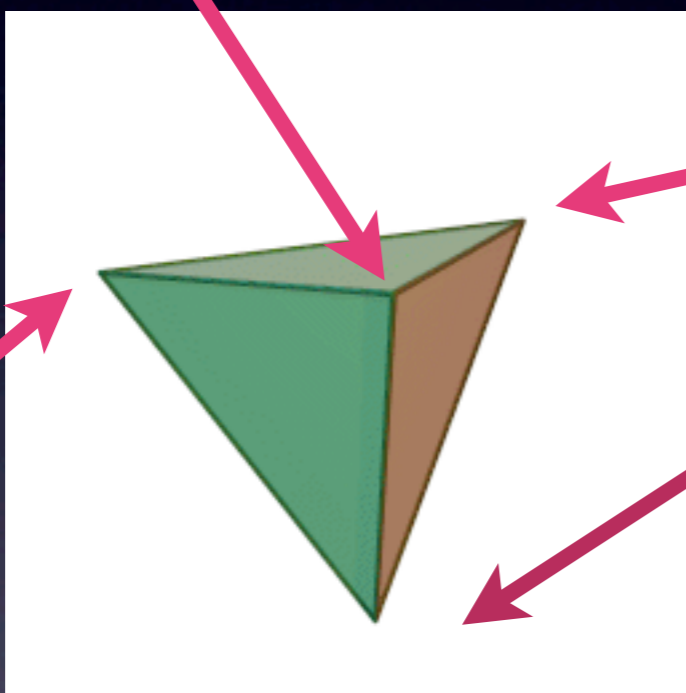


Presentation for Mr. Goodyear's Grade 4  
Class at Huron Street Public School

# Tetrahedron

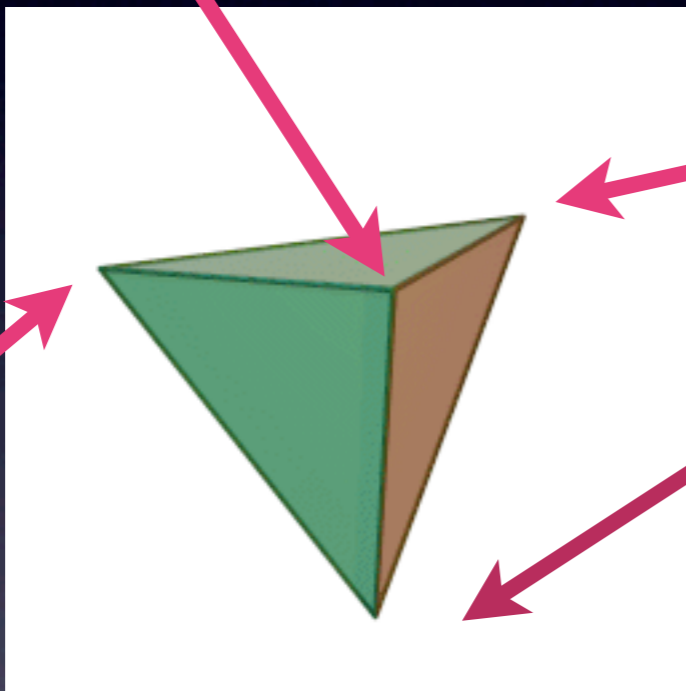


# Tetrahedron



Vertices

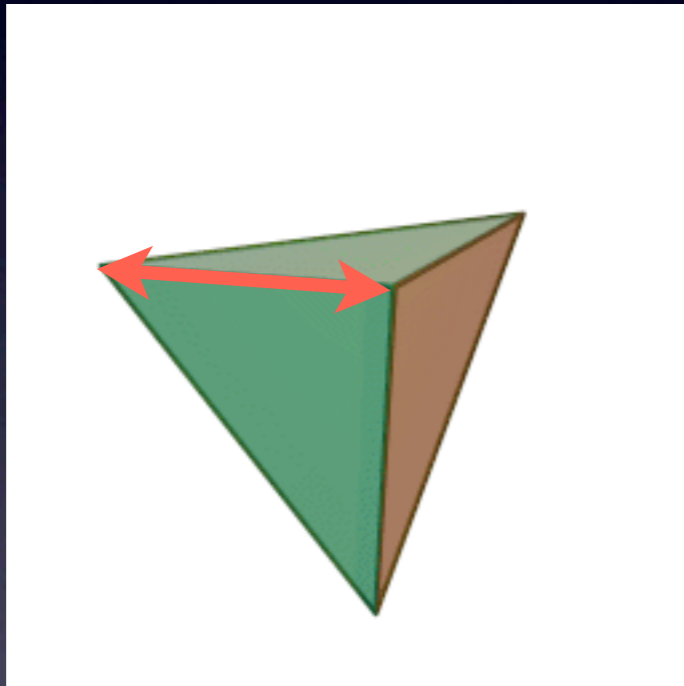
# Tetrahedron



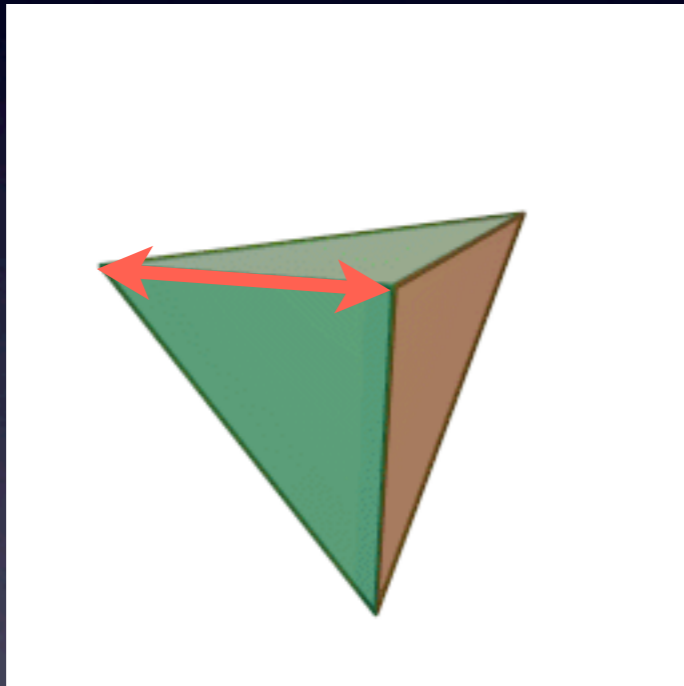
Vertices

$$V=4$$

# Tetrahedron



# Tetrahedron

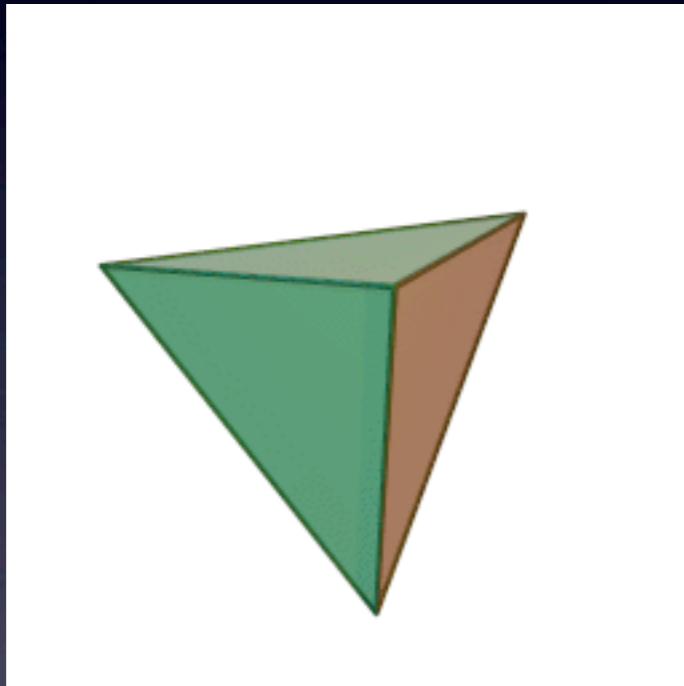


Edges

$$E=6$$

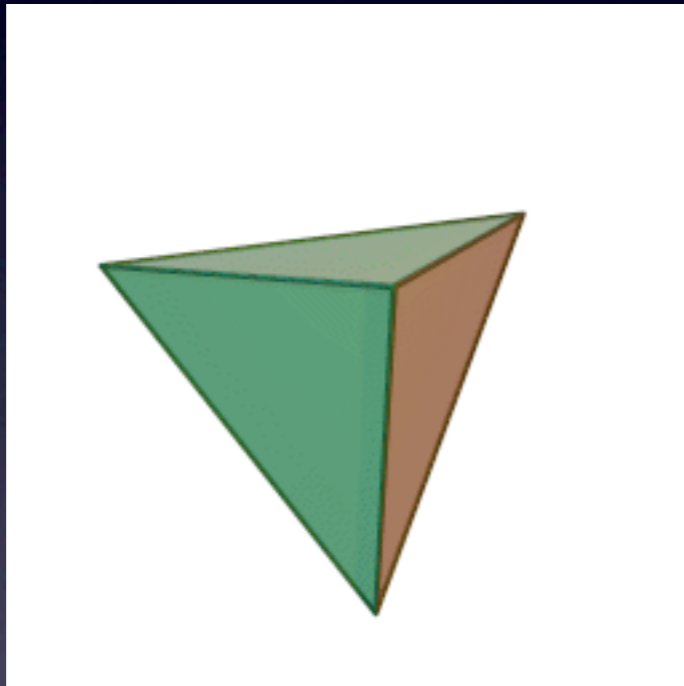
# Tetrahedron

Faces



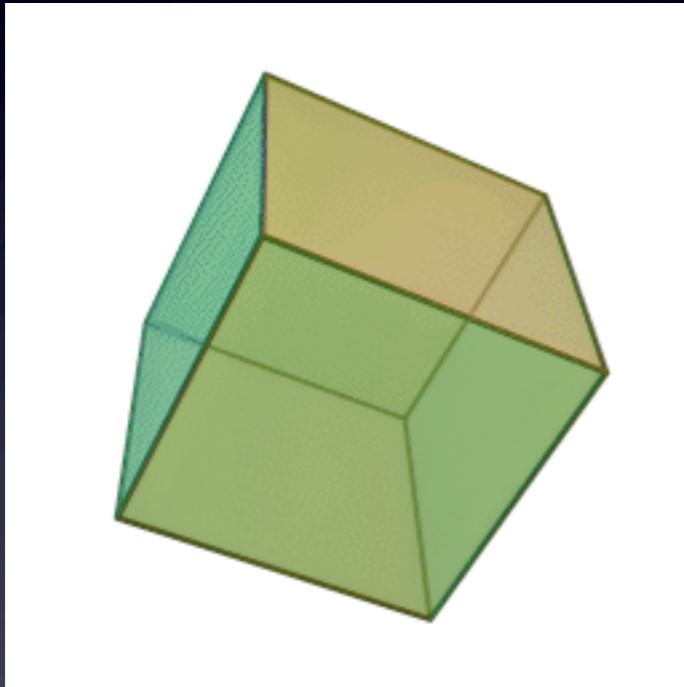
$$F=4$$

# Tetrahedron



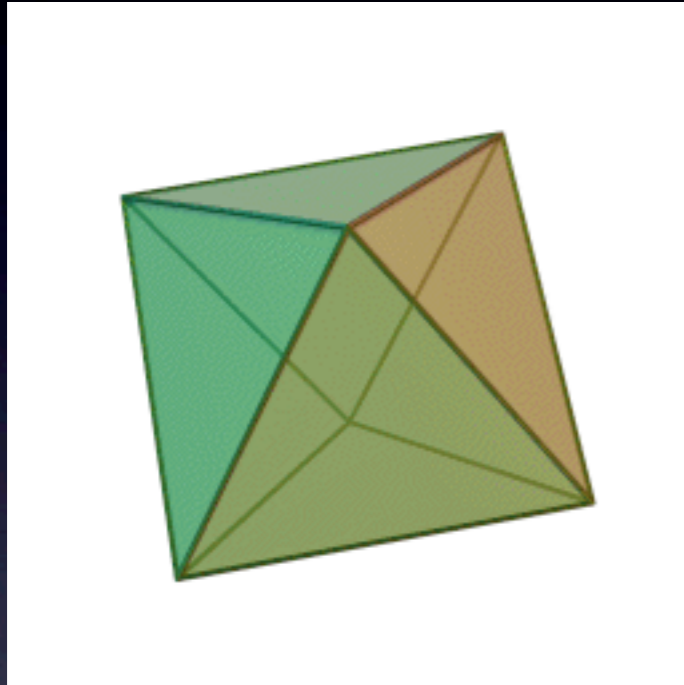
V	E	F	
4	6	4	

# Cube



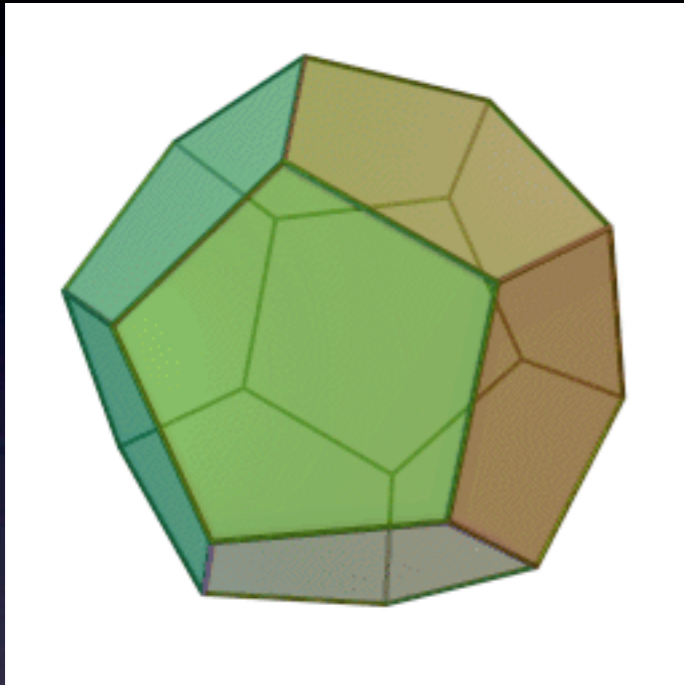
V	E	F	
8	12	6	

# Octahedron



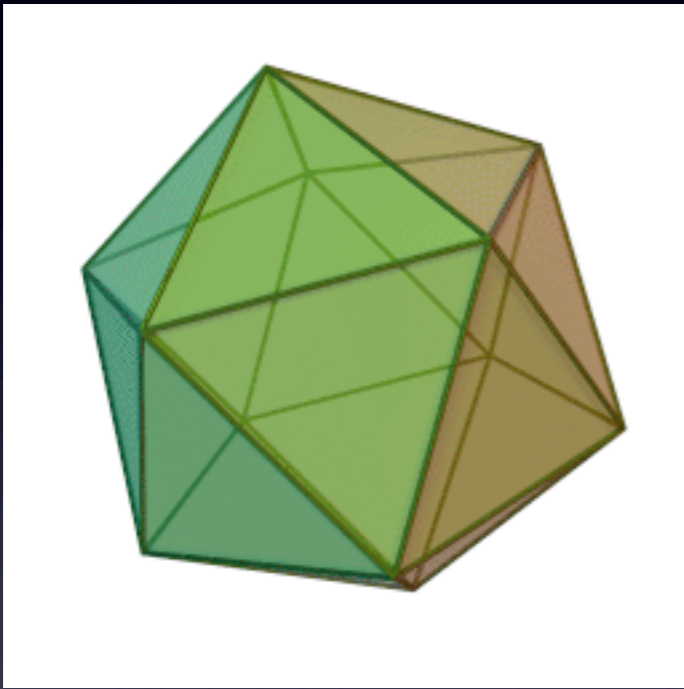
V	E	F	
6	12	8	

# Dodecahedron



V	E	F	
20	30	12	

# Icosahedron



V	E	F	
12	30	20	

# Find a Pattern!

Hedron	V	E	F	
Tetra	4	6	4	
Cube	8	12	6	
Octa	6	12	8	
Dodeca	20	30	12	
Icosa	12	30	20	

# Find a Pattern!

Hedron	V	E	F	?
Tetra	4	6	4	
Cube	8	12	6	
Octa	6	12	8	
Dodeca	20	30	12	
Icosa	12	30	20	

# Pattern?

Hedron	V	E	F	???
Tetra	4	6	4	
Cube	8	12	6	
Octa	6	12	8	
Dodeca	20	30	12	
Icosa	12	30	20	

# Pattern?

Hedron	V	E	F	V-E+F
Tetra	4	6	4	
Cube	8	12	6	
Octa	6	12	8	
Dodeca	20	30	12	
Icosa	12	30	20	

# Pattern?

Hedron	V	E	F	V-E+F
Tetra	4	6	4	2
Cube	8	12	6	
Octa	6	12	8	
Dodeca	20	30	12	
Icosa	12	30	20	

Hedron	V	E	F	V-E+F
Tetra	4	6	4	2
Cube	8	12	6	2
Octa	6	12	8	
Dodeca	20	30	12	
Icosa	12	30	20	

Hedron	V	E	F	V-E+F
Tetra	4	6	4	2
Cube	8	12	6	2
Octa	6	12	8	2
Dodeca	20	30	12	
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Hedron	V	E	F	V-E+F
Tetra	4	6	4	2
Cube	8	12	6	2
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Hedron	V	E	F	V-E+F
Tetra	4	6	4	2
Cube	8	12	6	2
Octa	6	12	8	2
Dodeca	20	30	12	2
Icosa	12	30	20	2

# Euler's Theorem

For ANY convex polyhedra

$$V - E + F = 2$$

# Euler's Theorem

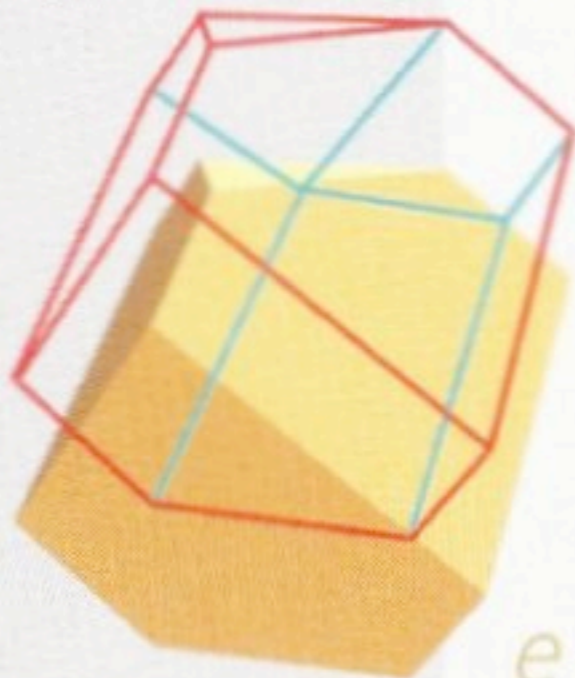
For ANY convex polyhedra

$$V - E + F = 2$$



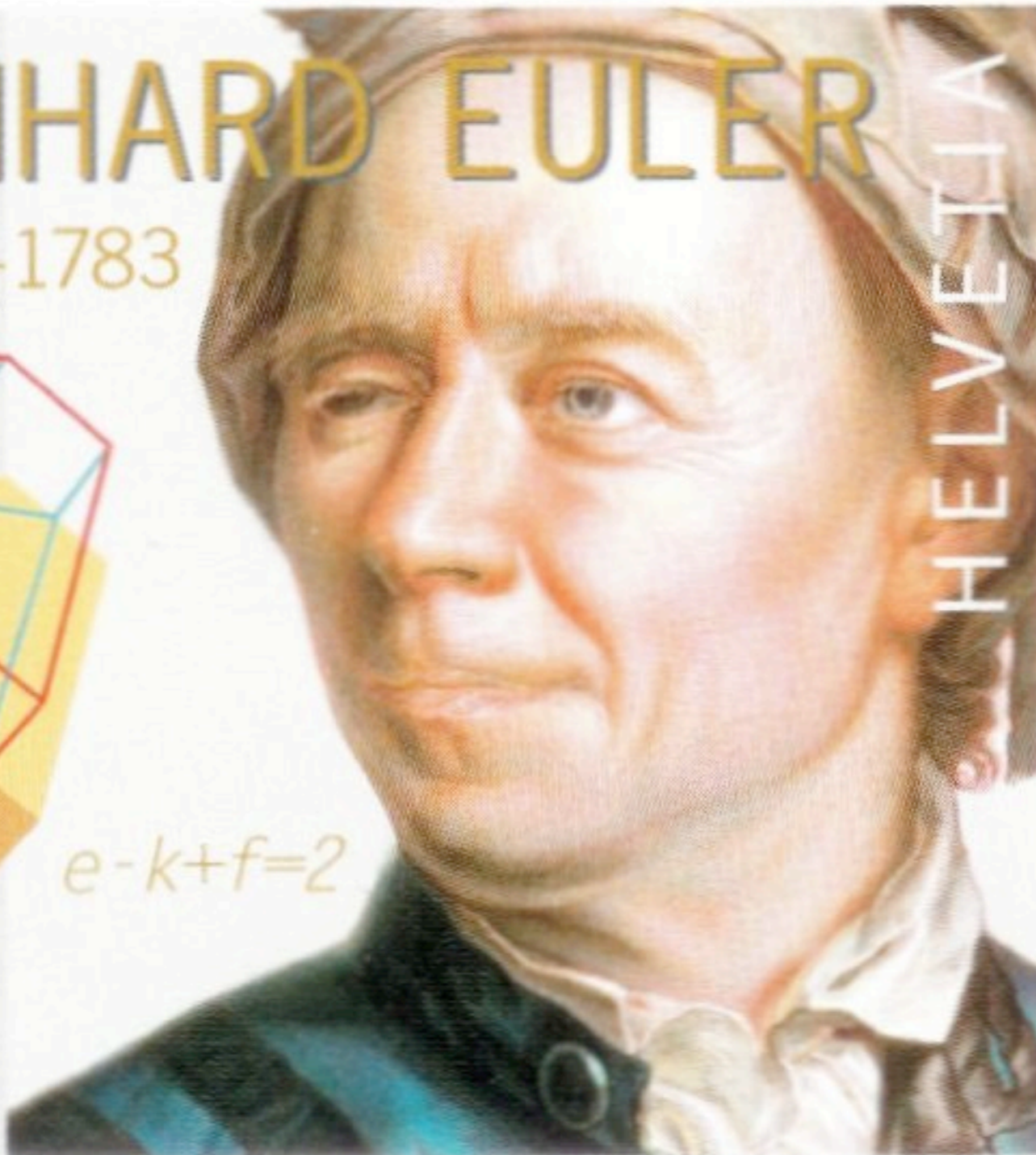
LEONHARD EULER

1707-1783



$$e - k + f = 2$$

130



HELVETIA

ANGELO BOOG

2007