

## PART 2:

## ANTIDERIVATIVES AND INDEFINITE INTEGRALS

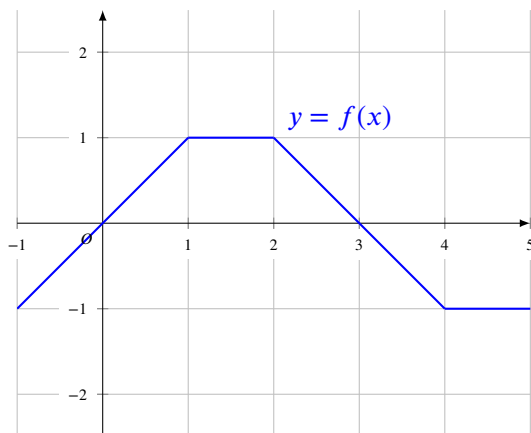
January 16<sup>th</sup>, 2019

## Initial Value Problem

Find a function  $f : \mathbb{R} \rightarrow \mathbb{R}$  such that

- For every  $x \in \mathbb{R}$ ,  $f''(x) = \sin x + x^2$ ,
- $f'(0) = 5$ ,
- $f(0) = 7$ .

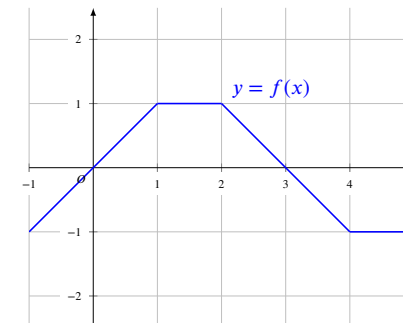
## Towards FTC



Compute:

- 1  $\int_0^1 f(t) dt$
- 2  $\int_0^2 f(t) dt$
- 3  $\int_0^3 f(t) dt$
- 4  $\int_0^4 f(t) dt$
- 5  $\int_0^5 f(t) dt$

## Towards FTC (continued)

Call  $F(x) = \int_0^x f(t) dt$ . This is a new function.

- Sketch the graph of  $y = F(x)$ .
- Using the graph you just sketched, sketch the graph of  $y = F'(x)$ .

1 Compute

$$\frac{d}{dx} [e^x \sin x], \quad \frac{d}{dx} [e^x \cos x].$$

2 Use the previous answer to Compute

$$\int e^x \sin x \, dx, \quad \int e^x \cos x \, dx.$$

1 Compute

$$\frac{d}{dx} [\arctan x], \quad \frac{d}{dx} \left[ \frac{x}{1+x^2} \right].$$

2 Use the previous answer to compute

$$\int \frac{1}{(1+x^2)^2} \, dx$$