

True or False?

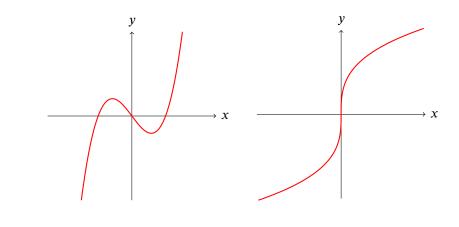
The position of the worm in terms of time is a function.

• What is the domain of f?

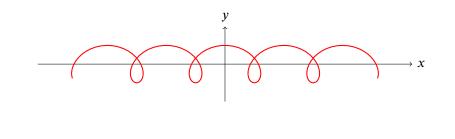
- **2** What is the codomain of f?
- **(3)** What is the range of f?
- **4** Does *f* admit an inverse?

Do these functions admit an inverse?

If so, sketch the graph of the inverse.

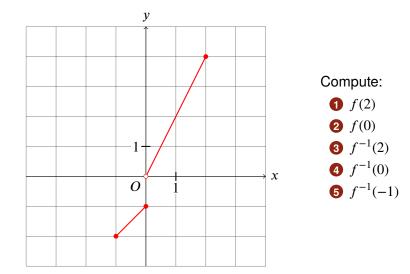


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Inverse function from a graph

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Absolute value and inverses

Define the function $f : \mathbb{R} \to \mathbb{R}$ by

h(x) = x|x| + 1

- Sketch the graph of *h* and explain briefly why it admits an inverse.
- **2** Compute $h^{-1}(-8)$.
- **3** Sketch the graph of h^{-1} .
- Find an equation for $h^{-1}(x)$.
- Verify that for every $t \in \mathbb{R}$, $h(h^{-1}(t)) = t$, and that for every $t \in \mathbb{R}$, $h^{-1}(h(t)) = t$.

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Logarithmic differentiation: be careful!

Let $f(x) = xe^{\sin(x)}$. We want to prove that $f'(x) = e^{\sin(x)} + x\cos(x)e^{\sin(x)}$ on \mathbb{R} .

What do you think about the following proof?

We have $\ln(f(x)) = \ln(xe^{\sin(x)}) = \ln(x) + \sin(x)$. Hence, by differentiating w.r.t. *x*, we get

$$\frac{f'(x)}{f(x)} = \frac{1}{x} + \cos(x)$$

Thus

$$f'(x) = f(x) \left(\frac{1}{x} + \cos(x)\right)$$
$$= xe^{\sin(x)} \left(\frac{1}{x} + \cos(x)\right)$$
$$= e^{\sin(x)} + x\cos(x)e^{\sin(x)}$$

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