MAT1300, fall 2011. Homework 6, Question 3
Adapted from Guillemin and Pollack page 63.
(a) Show that if $a>0$ then the solid hyperboloid $\left\{x^{2}+y^{2}-z^{2} \leq a\right\}$ is a manifold with boundary.
(b) Determine for which values of $a \in \mathbb{R}$ the intersection of the solid hyperboloid $\left\{x^{2}+y^{2}-z^{2} \leq a\right\}$ and the unit sphere $\left\{x^{2}+y^{2}+z^{2}=\right.$ $1\}$ is a manifold with boundary. What does this intersection look like?
(c) For which values of $a$ do the surfaces $\left\{x^{2}+y^{2}-z^{2}=a\right\}$ and $\left\{x^{2}+y^{2}+z^{2}=1\right\}$ intersect transversally?
(d) Explain the relation between your answers to parts (b) and (c).

