Let $V$ be a finite dimensional real vector space and let $T: V \rightarrow V$ be linear. Suppose that $T^{2}-3 T+2 I=0$ holds. Prove that $T$ is diagonalizable.

