

Let V be a finite dimensional real vector space and let $T : V \rightarrow V$ be linear. Prove that T is a scalar multiple of the identity if and only if $TS = ST$ holds for all linear transformations $S : V \rightarrow V$.