
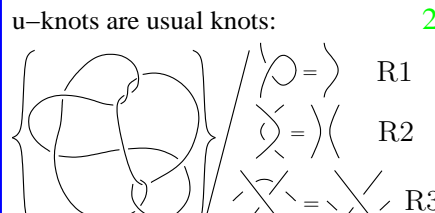

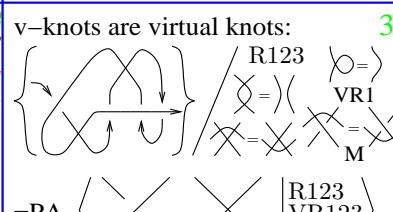
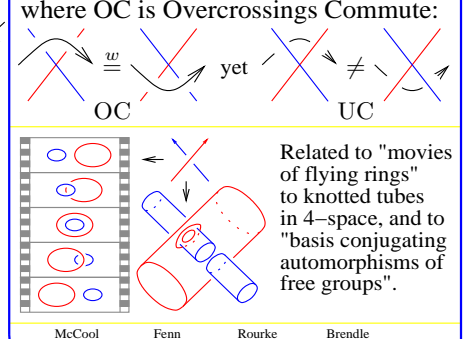
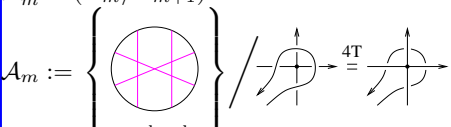
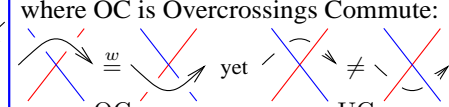
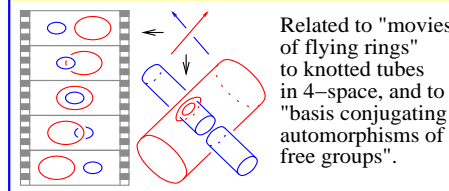

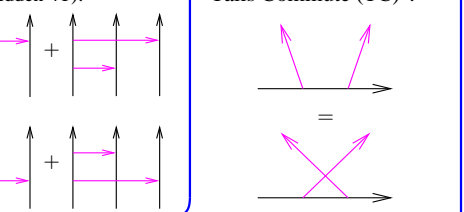
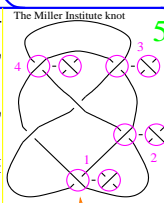

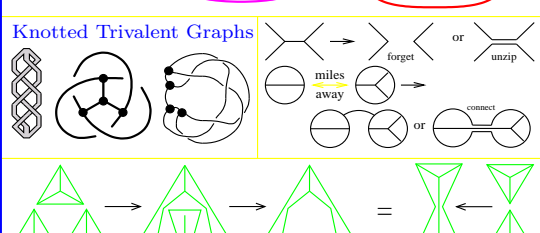


<p style="writing-mode: vertical-rl; transform: rotate(180deg);">topology</p>	<p>1  u-knots</p> <p>u-knots are usual knots:</p>  <p>Reidemeister</p> <p>"Knots in \mathbb{R}^3"</p>	<p>1+1 v-knots</p> <p>v-knots are virtual knots:</p>  <p>3</p> <p>0 legs</p> <p>Kauffman</p> <p>= Knots on surfaces, modulo stabilization:</p> 	<p>onto w-knots</p> <p>w is for welded, weakly v, and warmup:</p> <p>4 {w-knots} = {v-knots} / (OC)</p> <p>where OC is Overcrossings Commute:</p>  <p>Related to "movies of flying rings" to knotted tubes in 4-space, and to "basis conjugating automorphisms of free groups".</p> <p>McCool Goldsmith Fenn Rimanyi Rourke Satoh Brendle Hatcher</p>
	<p>combinatorics</p> <p>Extend any $V : \{\text{u-knots}\} \rightarrow \mathcal{A}$ to "singular u-knots" using $V(\times) := V(\times) - V(\times)$, and think "differentiation".</p> <p>Declare "V is of type m" iff $V^{(m+1)} \equiv 0$, think "polynomial of degree m".</p> <p>$W = V^{(m)}$ roughly determines V; $W \in \mathcal{A}_m^* = (\mathcal{K}_m / \mathcal{K}_{m+1})^*$ with</p>  <p>Need an expansion $Z : \{\text{u-knots}\} \rightarrow \mathcal{A} = \bigoplus \mathcal{A}_m$.</p> <p>Vassiliev Goussarov</p>	<p>5  All the same, except</p> <p>$V(\times) := V(\times) - V(\times)$</p> <p>$V(\times) := V(\times) - V(\times)$</p> <p>$\mathcal{A}^v := \{\text{"arrow diagrams"}\} / 6T$</p> <p>Need a $Z : \{\text{v-knots}\} \rightarrow \mathcal{A}^v$.</p> <p>The 6T Relation (and a hidden 4T):</p> 	<p>6  All the same, except</p> <p>$\mathcal{A}^w := \mathcal{A}^v / TC$</p> <p>Need a $Z : \{\text{w-knots}\} \rightarrow \mathcal{A}^w$.</p> <p>"Tails Commute (TC)":</p> 
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">low algebra</p>	<p>10 Similar</p> <p>with metrized Lie algebras replacing arbitrary Lie algebras</p> <p>Penrose Cvitanovic Vogel</p>	<p>9 Similar</p> <p>with Lie bi-algebras replacing arbitrary Lie algebras</p> <p>Haviv Leung</p>	<p>8 Theorem. $\mathcal{A}^w \cong \mathcal{A}^{wt} :=$</p>  <p>This screams, if you speak the language, LIE ALGEBRAS. And indeed we have</p> <p>Theorem. Given a finite dimensional Lie algebra \mathfrak{g}, there is $T : \mathcal{A}^w \rightarrow \mathcal{U}(I\mathfrak{g}) := \mathcal{U}(\mathfrak{g} \ltimes \mathfrak{g}_{ab}^*)$.</p>
	<p>11 Knots are the wrong objects to study in knot theory! They are not finitely generated and they carry no interesting operations.</p>  <p>Knotted Trivalent Graphs</p>  <p>Theorem (~). A homomorphic Z is the same as a "Drinfel'd Associator".</p> <p>Drinfel'd</p>	<p>13 Z is a Quantum Group?</p> <p>More precisely, a homomorphic Z ought to be equivalent to the Etingof-Kazhdan theory of deformation quantization of Lie bialgebras.</p> <p>Etingof Kazhdan</p> <p>Dror's Dream: Straighten and fatten this column.</p> <p>An Idle Question. Is there physics in this column?</p>	<p>12 Switch to w-knotted trivalent tangles,</p> <p>wKTT := $CA \langle \times, \times, Y \rangle$.</p> <p>Theorem (~). A homomorphic Z is equivalent to proving the Kashiwara-Vergne statement.</p> <p>Statement (~, KV, 1978) (proven Alekseev-Meinrenken, 2006). Convolutions of invariant functions on a group match with convolutions of invariant functions on its Lie algebra: for any finite dim. Lie group G with Lie algebra \mathfrak{g},</p> <p>$(\text{Fun}(G)^{\text{Ad } G}, \star) \cong (\text{Fun}(\mathfrak{g})^{\text{Ad } G}, \star)$.</p> <p>(Closely related to the "orbit method" of representation theory).</p> <p>Alekseev Torossian</p>