# Euler's Formula for Polyhedra 



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Presentation for Ms. Funston's Grade I Class at Huron Street Public School

## Tetrahedron



## Tetrahedron

## Tetrahedron



## Tetrahedron



## Tetrahedron



Edges
$E=6$

# Tetrahedron 

Faces
$F=4$

## Tetrahedron



## Cube



## Octahedron



## Dodecahedron



## Icosahedron



## Find a Pattern!

| Hedron | V | E | F |  |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 |  |
| Cube | 8 | 12 | 6 |  |
| Octa | 6 | 12 | 8 |  |
| Dodeca | 20 | 30 | 12 |  |
| Icosa | 12 | 30 | 20 |  |

## Find a Pattern!

| Hedron | V | E | F | $?$ |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 |  |
| Cube | 8 | 12 | 6 |  |
| Octa | 6 | 12 | 8 |  |
| Dodeca | 20 | 30 | 12 |  |
| Icosa | 12 | 30 | 20 |  |

## Pattern?

| Hedron | V | E | F | ??? |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 |  |
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## Pattern?

| Hedron | V | E | F | V-E+F |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 |  |
| Cube | 8 | 12 | 6 |  |
| Octa | 6 | 12 | 8 |  |
| Dodeca | 20 | 30 | 12 |  |
| Icosa | 12 | 30 | 20 |  |

## Pattern?

| Hedron | V | E | F | V-E+F |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 | 2 |
| Cube | 8 | 12 | 6 |  |
| Octa | 6 | 12 | 8 |  |
| Dodeca | 20 | 30 | 12 |  |
| Icosa | 12 | 30 | 20 |  |


| Hedron | V | E | F | V-E+F |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 | 2 |
| Cube | 8 | 12 | 6 | 2 |
| Octa | 6 | 12 | 8 |  |
| Dodeca | 20 | 30 | 12 |  |
| Icosa | 12 | 30 | 20 |  |


| Hedron | V | E | F | V-E+F |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 | 2 |
| Cube | 8 | 12 | 6 | 2 |
| Octa | 6 | 12 | 8 | 2 |
| Dodeca | 20 | 30 | 12 |  |
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| :---: | :---: | :---: | :---: | :---: |
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| Cube | 8 | 12 | 6 | 2 |
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| Hedron | V | E | F | V-E+F |
| :---: | :---: | :---: | :---: | :---: |
| Tetra | 4 | 6 | 4 | 2 |
| Cube | 8 | 12 | 6 | 2 |
| Octa | 6 | 12 | 8 | 2 |
| Dodeca | 20 | 30 | 12 | 2 |
| Icosa | 12 | 30 | 20 | 2 |

# Euler's Theorem 

For ANY convex polyhedra

$$
V-E+F=2
$$

# Euler's Theorem 

For ANY convex polyhedra

$$
V-E+F=2
$$




## Online Fun at Home

- Download (free) software from Google: http://sketchup.google.com
- Watch some of the help videos to learn how the buttons work.

