

# MAT194: CALCULUS

James Colliander

University of Toronto

Engineering Science

**1** COURSE INFORMATION

**2** CALCULUS DISTILLED

**3** SMOOTH STRUCTURE ON SMALL SCALES

# 1. COURSE INFORMATION

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Download it from the Portal ASAP!



**Basic Information for MAT194F Calculus  
Engineering Science  
2009**

## 1. Your Lecturers

J. Colliander  
Department of Mathematics  
6110 Bahen Center  
416 978 3645

P.C. Stangeby  
Institute for Aerospace Studies  
To arrange a meeting, please email: [pcs@starfire.utias.utoronto.ca](mailto:pcs@starfire.utias.utoronto.ca)  
Phone number: 416 667 7729

## 2. Lectures and Tutorials

# EVALUATION

- Two Term Tests 30%
- Tutorial Quizzes 20%
- Final Exam 50%

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Calibration





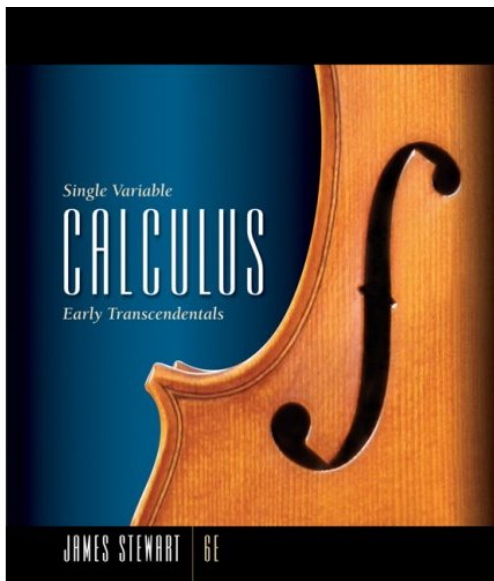
- Stewart, Calculus 6E
- Supplement: Barbeau-Stangeby



Read it this weekend!

Trig?

# TEXTBOOK



# LECTURE OVERVIEWS

## Basic Info Sheet

**L1** A brief introduction, including: the problem of defining the derivative in a rigorously logical way; problem with  $a/0$ ,  $0/0$ ,  $\infty$ ; basic idea of the limit; the use of  $\delta, \epsilon$  ideas; the difference between  $f(c)$  and  $\lim_{x \rightarrow c} f(x)$ .

T: A preview of calculus, pages 2-9; Sec. 2.1.

TP: page 65: 3, 5

S: Sec. 1.

**L2, L3, L4** The real number system, including: field and order axioms; absolute value; function; roots; intervals; increasing/decreasing; inequalities; intervals described by inequalities; inequalities involving  $\delta, \epsilon$ ; triangle inequality. A brief introduction to trigonometry.

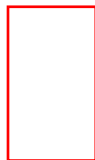
T: Secs. 1.1, 1.2, 1.3, Appendix D.

TP: pages 20-23: 18, 21, 23, 24, 31, 35, 39, 44, 56, 59, 63, 68; pages 34-37: 1, 2, 3, 4, 10, 15, 20, 23; pages 43-45: 3, 6, 7, 9, 17, 24, 26, 31, 38, 43, 58; pages 51-52: 2, 5, 24, 29,

## 2. CALCULUS DISTILLED

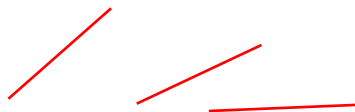
## 2. CALCULUS DISTILLED

- Rectangle: Area = Base  $\times$  Height.
- Slope:  $\frac{\text{Rise}}{\text{Run}}$
- Limit:  $\lim_{x \rightarrow c} f(x) = ?$ .



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Key Ingredient: The spice!

### 3. SMOOTH STRUCTURE ON SMALL SCALES



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**Calculus:** A **Toolbox** for studying objects which behave nicely enough on small scales.

- Determinism; Time Evolution; Idea of Rate
- Optimization
- Smooth Geometry

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???



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← Cheapest? Best?

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Nonsmooth Examples

# INVENTORS OF CALCULUS

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**Gottfried Leibniz**

Crushed by Newton....



# INVENTORS OF CALCULUS

## Isaac Newton



# ISAAC NEWTON!

French mathematician Joseph-Louis Lagrange often said that

- J.L Lagrange: Newton was the greatest genius who ever lived, and once added that he was also "the most fortunate, for we cannot find more than once a system of the world to establish."
- Newton was rather more modest: In a letter to Robert Hooke, "If I have seen further it is by standing on the shoulders of Giants". (Though some historians think the above quote was an attack on Hooke who was short and hunchbacked, rather than or in addition to a statement of modesty.)
- I do not know what I may appear to the world, but to myself I seem to have been only like a boy playing on the sea-shore, and diverting myself in now and then finding a smoother pebble or a prettier shell than ordinary, whilst the great ocean of truth lay all undiscovered before me.



